Tribhuwan University Institute of Science and Technology 2077

Bachelor Level / First Semester / Science **Computer Science and Information Technology(MTH112)** ((TU CSIT) Mathematics I (Calculus)) Candidates are required to give their answers in their own words as far as practicable. The figures in the margin indicate full marks.

Group A(10 x 3 = 30)

Attempt any THREE questions.

1(a) If f(x) = x2 then find

1(b) Dry air is moving upward. If the ground temperature is 20⁰ and the temperature at a height of 1km is 10⁰ C, express the temperature T in ⁰C as a function of the height h (in kilometers), assuming that a linear model is appropriate. (b)Draw the graph of the function in part(a). What does the slope represent? (c) What is the temperature at a height of 2km?(5)

1(c). Find the equation of the tangent to the parabola $y = x^2 + x + 1$ at (0, 1)

2(a)A farmer has 2000 ft of fencing and wants to fence off a rectangular field that borders a straight river. He needs no fence along the river. What are the dimentions of the field that has the largest area?[5]

2(b)Sketch the curve[5]

$$y = \frac{1}{x - 3}$$

3(a)Show that the converges

(b) If f(x, y) = xy/(x² + y²), does f(x, y) exist, as (x, y) \rightarrow (0, 0)?[3]

3(c) A particle moves in a straight line and has acceleration given by $a(t) = 6t^2 + 1$. Its initial velocity is 4m/sec and its initial displacement is s(0) = 5cm. Find its position function s(t).[5]

 $\int_{1}^{\infty} \frac{1}{x^2} \int_{1}^{\infty} \frac{1}{x}$ and diverges .[2]

4. (a) Evaluate[5]

$$\int_{3}^{2} \int_{0}^{\frac{\pi}{2}} (y + y^2 \cos x) dx dy$$

4(b) Find the Maclaurin's series for cos x and prove that it represents cos x for all x.[5]

Group B(10 x 5 = 50)

Attempt any TEN questions.

5. If $f(x) = x^2 - 1$, g(x) = 2x + 1, find fog and gof and domain of fog.

6. Define continuity of a function at a point
$$x = a$$
. Show that the function $f(x) = a$

Full marks: 80 Pass marks: 32 Time: 3 hours



is continuous on the interval[1, -1].

7. State Rolle's theorem and verify the Rolle's theorem for $f(x) = x^3 - x^2 - 6x + 2$ in [0, 3].

8. Find the third approximation x_3 to the root of the equation $f(x) = x^3 - 2x - 7$, setting $x^1 = 2$.

9. Find the derivatives of $r(t) = (1 + t^2)i - te^{-t}j + sin 2tk$ and find the unit tangent vector at t=0.

10. Find the volume of the solid obtained by rotating about the y-axis the region between y = x and $y = x^2$.

11. Solve: y" + y' = 0, y(0) = 5, y($\pi/4$) = 3

$$\sum_{n=0}^{\infty} \frac{1}{1+n^2}$$

12. Show that the series

converges.

13. Find a vector perpendicular to the plane that passes through the points:p(1, 4, 6), Q(-2, 5, -1) and R(1. -1, 1)

14. Find the partial derivative of $f(x, y) = x^3 + 2x^3y^3 - 3y^2 + x + y$, at (2,1).

15. Find the local maximum and minimum values, saddle points of $f(x,y) = x^4 + y^4 - 4xy + 1$.